

Teacher: CORE
PreCalc Year: 2017-18
Course: Month: All
PreCalc Months

Teacher: CORE
PreCalc Year: 2017-18
Course: Month: All
PreCalc Months

Teacher: CORE
PreCalc Year: 2017-18
Course: Month: All
PreCalc Months

Teacher: CORE
PreCalc Year: 2017-18
Course: Month: All
PreCalc Months

S Prerequisites

e Essential

Essential Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
p t e m	Real Numbers	Order real numbers, use inequalities, evaluate algebraic expressions		Quiz: P1 - P2 Assessment of learning			2.1.11.A-Use operations (e.g., opposite, reciprocal, absolute value, raising to a power, finding roots, finding logarithms).
				Quiz: P3 - P4 Performance Assessment			2.2.11.A-Develop and use computation concepts, operations and procedures with real numbers in problem-solving situations.
				Quiz: P5 - P6 Performance Assessment			2.2.11.C-Construct and apply mathematical models, including lines and curves of best fit, to estimate values of related quantities.
				Test: P1 - P8 Performance Assessment			
b e r O Functions and Graphing	Exponents and Radicals	Apply properties of exponents					
		Apply properties of radicals					
	Polynomials and Factoring	Add, subtract, and multiply polynomials					
		Factor polynomials					
	Rational expressions	Add, subtract, multiply and divide rational expressions					
	Solving Equations	Solve polynomial equations, equations involving radicals, and absolute value equations					
	Solving Inequalities	Solve inequalities					
	Graphical representation of data	Use the coordinate plane to model and solve real-life problems					

c t o b e r	Essential Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
		Graphs of equations	Sketch the graph of an equation using a table of values, intercepts and symmetry Graph equations using a graphing calculator		Quiz: 1.2 - 1.3 Performance Assessment Quiz 1.4 - 1.5 Quiz 1.6 - 1.8 Test 1.1 - 1.8			2.8.11.A-Analyze a given set of data for the existence of a pattern and represent the pattern algebraically and graphically. 2.8.11.Q-Represent functional relationships in tables, charts and graphs. 2.8.11.S-Analyze properties and relationships of functions (e.g., linear, polynomial, rational, trigonometric, exponential, logarithmic). 2.8.11.T-Analyze and categorize functions by their characteristics.
		Lines	Find and use the slopes of lines to write and graph linear equations in two variables Determine whether lines are parallel or perpendicular using slope Solve problems using linear equations Interpret slope as a rate of change					2.8.11.K-Select, justify and apply an appropriate technique to graph a linear function in two variables, including slope-intercept, x- and y-intercepts, graphing by transformations and the use of a graphing calculator. 2.8.11.L-Write the equation of a line when given the graph of the line, two points on the line, or the slope of the line and a point on the line. 2.8.11.M-Given a set of data points, write an equation for a line of best fit. M11.D.3.1-Describe and/or determine change. (Reference: 2.8.8.J, 2.11.8.B) M11.D.3.2-Compute and/or use the slope of a line. (Reference: 2.8.11.J, 2.8.11.L)
		Functions	Evaluate functions and find their domain and range Evaluate difference quotients					2.8.11.O-Determine the domain and range of a relation, given a graph or set of ordered pairs. 2.8.11.Q-Represent functional relationships in tables, charts and graphs. 2.8.11.R-Create and interpret functional models. 2.8.11.S-Analyze properties and relationships of functions (e.g., linear, polynomial, rational, trigonometric, exponential, logarithmic). 2.8.11.T-Analyze and categorize functions by their characteristics.

Graphs of
Functions

Analyze graphs of functions
including step functions, piecewise
functions, and even and odd
functions
Determine domain and range,
intervals of increase and decrease,
zeros, and maxima and minima

Use the vertical line test for
functions

Transformations
of Graphs

Identify and graph translations,
reflections, and non-rigid
transformations of functions
Describe transformations from a
graph and from the function
equation

M11.D.1.1-Analyze and/or use patterns or
relations. (Reference: 2.8.11.Q; 2.8.11.A;
2.8.11.0)

2.2.12.A-Determine and explain the meaning of
the zeros of functions model from real life
situations.

2.8.11.A-Analyze a given set of data for the
existence of a pattern and represent the pattern
algebraically and graphically.

2.8.11.O-Determine the domain and range of a
relation, given a graph or set of ordered pairs.

2.8.11.Q-Represent functional relationships in
tables, charts and graphs.

2.8.11.T-Analyze and categorize functions by their
characteristics.

2.8.12.K-Create, write, and solve real life
problems that demonstrate an understanding of
appropriate function models.

2.11.11.A-Determine maximum and minimum
values of a function over a specified interval.

2.11.11.B-Interpret maximum and minimum
values in problem situations.

2.11.12.B-Describe the meaning of maximum or
minimum values of a function and how it applies
to a real life situation.

M11.D.1.1-Analyze and/or use patterns or
relations. (Reference: 2.8.11.Q; 2.8.11.A;
2.8.11.0)

2.8.11.A-Analyze a given set of data for the
existence of a pattern and represent the pattern
algebraically and graphically.

2.8.11.Q-Represent functional relationships in
tables, charts and graphs.

2.8.11.T-Analyze and categorize functions by their
characteristics.

Operations on Functions Find arithmetic combinations and compositions of functions

Decompose a function

Inverse Functions Find the inverse of a function graphically and algebraically

Determine the domain and range of a function and its inverse

Direct, Inverse, and Joint Variation Write and apply algebraic models for direct, inverse, and joint variation
Solve problems from science (Chemistry and Physics) using direct or inverse variation

2.8.11.S-Analyze properties and relationships of functions (e.g., linear, polynomial, rational, trigonometric, exponential, logarithmic).
M11.D.2.2-Simplify expressions involving polynomials. (Reference: 2.8.11.S)
2.8.11.A-Analyze a given set of data for the existence of a pattern and represent the pattern algebraically and graphically.
2.8.11.O-Determine the domain and range of a relation, given a graph or set of ordered pairs.

2.8.11.Q-Represent functional relationships in tables, charts and graphs.
M11.D.1.1-Analyze and/or use patterns or relations. (Reference: 2.8.11.Q; 2.8.11.A; 2.8.11.O)
2.8.11.A-Analyze a given set of data for the existence of a pattern and represent the pattern algebraically and graphically.
2.8.11.B-Give examples of patterns that occur in data from other disciplines.

2.8.11.P-Analyze a relation to determine whether a direct or inverse variation exists and represent it algebraically and graphically.
2.8.12.J-Solve problems involving direct, inverse and joint variation.
2.8.12.K-Create, write, and solve real life problems that demonstrate an understanding of appropriate function models.
M11.A.2.1-Apply ratio and/or proportion in problem-solving situations. (Reference: 2.2.11.A, 2.8.11.P)

N Polynomial Functions

o	Essential						
	Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources
v		Quadratic functions	Analyze equations and graphs of quadratic functions to determine the vertex, axis of symmetry, and intercepts		QUIZ: 2.1 - 2.3		2.8.11.A-Analyze a given set of data for the existence of a pattern and represent the pattern algebraically and graphically.

e			QUIZ: 2.4 - 2.7	2.8.11.N-Solve linear, quadratic and exponential equations both symbolically and graphically.
m			TEST: 2.1 - 2.7	2.8.11.S-Analyze properties and relationships of functions (e.g., linear, polynomial, rational, trigonometric, exponential, logarithmic).
b		Write quadratic functions in standard form and determine characteristics of the graph		2.11.11.A-Determine maximum and minimum values of a function over a specified interval.
e		Solve problems involving quadratic functions and maxima and minima		2.11.12.B-Describe the meaning of maximum or minimum values of a function and how it applies to a real life situation.
r				M11.D.4.1-Interpret and/or use linear, quadratic and/or exponential functions and their equations, graphs or tables. (Reference: 2.8.11.K, 2.8.11.Q.)
	Polynomial functions	Define polynomial functions and graph polynomial functions using the leading coefficient test		2.8.11.A-Analyze a given set of data for the existence of a pattern and represent the pattern algebraically and graphically.
		Graph transformations of polynomial functions		2.8.11.Q-Represent functional relationships in tables, charts and graphs.
		Define continuity		2.8.11.T-Analyze and categorize functions by their characteristics.
	Polynomial division	Determine the quotient of polynomials using division and synthetic division		2.8.12.I-Collect and model real life data using polynomial functions, exponential and power functions.
		Use the Remainder and Factor Theorems		2.8.11.S-Analyze properties and relationships of functions (e.g., linear, polynomial, rational, trigonometric, exponential, logarithmic).
	Zeros of Polynomial Functions	Perform operations with complex numbers		M11.D.2.2-Simplify expressions involving polynomials. (Reference: 2.8.11.S)
		Determine the number of rational and real zeros of polynomial functions, and find the zeros using factoring and the graphing calculator		2.2.12.A-Determine and explain the meaning of the zeros of functions model from real life situations.

Rational Functions

Essential Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
	Rational Functions and Asymptotes	Determine the domain and range of rational functions Define rational functions and horizontal and vertical asymptotes					2.8.11.A-Analyze a given set of data for the existence of a pattern and represent the pattern algebraically and graphically. 2.8.11.O-Determine the domain and range of a relation, given a graph or set of ordered pairs. 2.8.11.Q-Represent functional relationships in tables, charts and graphs. M11.D.1.1-Analyze and/or use patterns or relations. (Reference: 2.8.11.Q; 2.8.11.A; 2.8.11.0)
	Graphs of Rational Functions	Analyze and sketch the graphs of rational functions Find vertical and horizontal asymptotes					2.8.11.A-Analyze a given set of data for the existence of a pattern and represent the pattern algebraically and graphically. 2.8.11.Q-Represent functional relationships in tables, charts and graphs. M11.D.1.1-Analyze and/or use patterns or relations. (Reference: 2.8.11.Q; 2.8.11.A; 2.8.11.0)
	Partial Fractions	Find partial fraction decomposition of rational expressions					2.2.11.A-Develop and use computation concepts, operations and procedures with real numbers in problem-solving situations. M11.A.2.1-Apply ratio and/or proportion in problem-solving situations. (Reference: 2.2.11.A, 2.8.11.P) M11.A.3.1-Apply the order of operations in computation and in problem-solving situations. (Reference: 2.2.8.A)

D Exponential and Logarithmic Functions

Essential Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
c	Exponential Functions and their graphs	Define, evaluate, and graph exponential functions with base a		Quiz: 3.1 - 3.3			2.1.11.A-Use operations (e.g., opposite, reciprocal, absolute value, raising to a power, finding roots, finding logarithms).

e		Define, evaluate, and graph the natural exponential function	Quiz: 3.4 - 3.5	2.8.11.N-Solve linear, quadratic and exponential equations both symbolically and graphically.
m			Test: 3.1 - 3.5	2.8.11.Q-Represent functional relationships in tables, charts and graphs.
b				2.8.11.S-Analyze properties and relationships of functions (e.g., linear, polynomial, rational, trigonometric, exponential, logarithmic).
e				2.8.11.T-Analyze and categorize functions by their characteristics.
r	Logarithmic Functions and their Graphs	Define, graph and evaluate logarithmic functions with base a Define, graph, and evaluate the natural logarithmic function		2.1.11.A-Use operations (e.g., opposite, reciprocal, absolute value, raising to a power, finding roots, finding logarithms). 2.8.11.N-Solve linear, quadratic and exponential equations both symbolically and graphically.
	Properties of logarithms	Use the properties of logarithms to evaluate, expand, and condense logarithmic expressions		2.8.11.S-Analyze properties and relationships of functions (e.g., linear, polynomial, rational, trigonometric, exponential, logarithmic). 2.1.11.A-Use operations (e.g., opposite, reciprocal, absolute value, raising to a power, finding roots, finding logarithms).
	Exponential and logarithmic equations	Solve exponential and logarithmic equations		2.1.11.A-Use operations (e.g., opposite, reciprocal, absolute value, raising to a power, finding roots, finding logarithms).
	Exponential and logarithmic models	Use exponential growth and decay, logistic growth, and logarithmic models to solve problems		2.8.11.R-Create and interpret functional models. 2.11.11.C-Graph and interpret rates of growth/decay.

J Trigonometry

a	Essential Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
n		Angle measures in degrees and radians	Define and use radian and degree measure of angles Convert angle measures using degrees and radians		Quiz: 4.1 - Performance Assessment Quiz: 4.2 Assessment of learning			2.3.11.B-Measure and compare angles in degrees and radians. M11.B.2.1-Use and/or compare measurements of angles. (Reference: 2.3.11.a, 2.3.11.B)
u					Test: 4.1 - 4.4 Assessment of learning			

ry

Quiz: 4.5 - 4.6 Assessment of learning
Test: 4.5 - 4.8 Assessment of learning

Right triangle trigonometry	Review right triangle definitions of trig functions and trig ratios in special right triangles Solve application problems involving right triangle trig
Trigonometric Functions	Evaluate trig functions using the unit circle and reference angles
Graphs of Trig Functions	Graph the sine, cosine, tangent, cosecant, secant, and cotangent functions Graph translations of the sine and cosine functions
Inverse Trig Functions	Define, evaluate, and graph inverse trig functions Evaluate compositions of inverse trig functions

2.10.11.B-Identify, create and solve practical problems involving right triangles using the trigonometric functions and the Pythagorean Theorem.

2.10.11.B-Identify, create and solve practical problems involving right triangles using the trigonometric functions and the Pythagorean Theorem.

F Trigonometric Identities and Formulas

e	Essential Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
b		Trig Identities	Review fundamental trig identities to evaluate trig functions and simplify trig expressions.		Quiz 5.1 - 5.2 Assessment of Learning			2.5.11.C-Present mathematical procedures and results clearly, systematically, succinctly and correctly.
rua			Verify trig identities		Quiz: 5.3 - 5.5 Assessment of learning Test: 5.1 - 5.5 Assessment of Learning			
		Trig Equations	Solve trig equations using algebra techniques and inverse trig functions					
r		Sum and Difference	Derive sum and difference formulas					

y	formulas	Evaluate trig functions and solve trig equations using these formulas
	Multiple angle and product sum formulas	Simplify and evaluate trig expressions using multiple angle and product sum formulas
M Applications of Trigonometry		

a	Essential							
	Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
r		Law of Sines	Solve triangles using the Law of Sines		Quiz: 6.1 - 6.2 Assessment of Learning			2.2.11.C-Construct and apply mathematical models, including lines and curves of best fit, to estimate values of related quantities.
c			Find the area of triangles		Quiz: 6.3 - 6.5 Assessment of Learning			2.3.11.B-Measure and compare angles in degrees and radians.
h					Test: 6.1 - 6.5 Assessment of Learning			2.4.11.C-Determine the validity of an argument.
								2.4.11.E-Demonstrate mathematical solutions to problems (e.g., in the physical sciences).
								2.5.11.A-Select and use appropriate mathematical concepts and techniques from different areas of mathematics and apply them to solving non-routine and multi-step problems.
		Law of Cosines	Solve triangles using the Law of Cosines					
		Vectors	Write the component form of vectors and perform vector operations Represent vectors as directed line segments and as rays on the coordinate plane Define and apply vector addition and scalar multiplication Find the direction angle of vectors					
			Solve application problems using vectors					

A Sequences
and Series

p	Essential							
	Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
r		Sequences and Series	Use sequence, factorial, and summation notation to write the terms and sum of a sequence		Quiz: 9.1 - 9.3 Assessment of learning Quiz: 9.4 - 9.7 Assessment of learning Test: 9.1 - 9.7 Assessment of learning			2.4.11.B-Construct valid arguments from stated facts. 2.4.11.E-Demonstrate mathematical solutions to problems (e.g., in the physical sciences). 2.5.11.A-Select and use appropriate mathematical concepts and techniques from different areas of mathematics and apply them to solving non-routine and multi-step problems. 2.5.11.B-Use symbols, mathematical terminology, standard notation, mathematical rules, graphing and other types of mathematical representations to communicate observations, predictions, concepts, procedures, generalizations, ideas and results. 2.5.11.C-Present mathematical procedures and results clearly, systematically, succinctly and correctly. 2.7.11.A-Compare odds and probability. 2.7.11.D-Use experimental and theoretical probability distributions to make judgments about the likelihood of various outcomes in uncertain situations. 2.7.11.E-Solve problems involving independent simple and compound events.
i								
l		Arithmetic sequences Geometric sequences Mathematical induction Binomial Theorem	Solve problems involving arithmetic sequences and series Solve problems involving geometric sequences and series Use mathematical induction to prove a statement Use binomial throrom and Pascal's triangle to calculate binomial coefficients					

Counting	Solve counting problems using Fundamental Counting Principle permutations and combinations
Probability	Find probabilities of mutually exclusive events, independent events and complements of events

M Systems of Equations and Matrices & Determinants

a	Essential Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
y		Solving systems of equations	To solve systems of equations by substitution, elimination and graphing		Quiz: 7.1 - 7.2 Quiz: 7.3 - 7.4 Test: 7.1 - 7.4 Assessment of learning			2.2.11.F-Demonstrate skills for using computer spreadsheets and scientific and graphing calculators. 2.5.11.A-Select and use appropriate mathematical concepts and techniques from different areas of mathematics and apply them to solving non-routine and multi-step problems. 2.5.11.C-Present mathematical procedures and results clearly, systematically, succinctly and correctly.
		Multivariable linear systems Solving Systems of Inequalities	Solve multivariable systems of equations Graph inequalities in two variables and solve systems of inequalities					
		Operations with Matrices	Add and subtract matrices Multiply matrices by real numbers Find the product of two matrices		Quiz: 8.1 - 8.2 Assessment of learning Quiz: 8.3 - 8.5 Assessment of learning Test: 8.1 - 8.5 Assessment of learning			
		Inverse Matrices	Find the inverse of a matrix and use inverse matrices to solve systems of equations					
		Determinants	Find determinants of a 2x2 matrix					

Use Cramer's Rule to solve systems of equations

Use determinants and matrices to solve problems involving area of a triangle

J Analytic
Geometry

J u n e	Essential							
	Questions	Content	Knowledge and Skills	Vocabulary	Assessments	Lessons	Resources	Standards
		Conics	Define and describe circles, parabolas, ellipses, and hyperbolas					
		Transformation of Conics	Write equations of conics Graph conics Write and graph equations of conics with vertical or horizontal translations					
		Parametric Equations	Evaluate, graph and write parametric equations					